Since the diagonals bisect each other, LMNK is a parallelogram. That eliminates choice D, since a trapezoid is not a parallelogram. We also know the diagonals are congruent which means LMNK is a rectangle.

#2

If MEQT is a parallelogram, then its opposite angles are congruent. Therefore:

$$6x + 12 = 5x + y$$

$$5implify \rightarrow -5x \qquad -5x$$

$$x + 12 = y$$

If you substitute the x, y pairs from the choices into x+12=y, you find that choices B and D are possible solutions. To eliminate another choice, use the fact that MEQT is not a rectangle and therefore does not have 90° angles.

If x=13 (choice B) then: If x=15 (choice D) then: $m\angle E = (6x+12)$ = (6(13)+12) = 78+12 $= 90^{\circ}$ $= 102^{\circ}$

Correct choice, since not a right angle.

#3

There is not enough information to determine if all four sides of SRPQ are congruent, so instead we will check to see if the diagonals are perpendicular. If they are, then SRPQ is a thombus. Consider the Δ with side lengths 10, 24, and 26. See if the lengths form a Pythagorean triple.

$$10^{2} + 24^{2} = 26^{2}$$

$$100 + 576 = 676$$

$$676 = 676$$

Since the Pythagorean relationship holds true, 5P L QR and therefore SRPQ is a thombus.

#4 VT = 28

Since VWTR is a rectangle, its diagonals bisect each other and are congruent. So if WZ = 14, then ZR = 14 as well, which makes WR = 28. If the diagonals are equal then $VT \cong WR$ and is 28 as well.

#5 62°

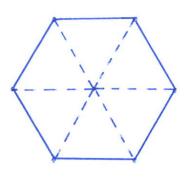
The exterior angles of a polygon always add up to 360. Therefore:

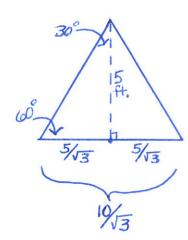
$$X + 88 + 88 + 32 + 90 = 360^{\circ}$$

 $X + 298 = 360^{\circ}$
 $X = 62^{\circ}$

#6 86.6 sq. feet

Notice that a regular hexagon is composed of six congruent triangles. If you find the area of one \triangle , you could multiply it by 6 to get the total area.



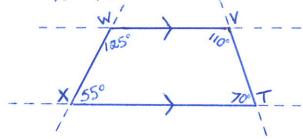


They are equilateral triangles (a regular hexagon's interior angles are 120°, so the triangles' base angles must be half that $\rightarrow 60^{\circ}$). Using the $30^{\circ}-60^{\circ}-90^{\circ}$ \triangle relationship (see diagram) we know that half the base is $5/\sqrt{3}$ and therefore the entire base length is $10/\sqrt{3}$.

Area = base height =
$$(10/\sqrt{3})(5) = 14.434$$

The interior angles of any quadrilateral total 360°. $m \times X + 70 + 110 + 125 = 360$ $m \times X + 305 = 360$ $m \times X = 55°$

Note that both pairs of adjacent angles are supplementary. 70+110=180, 55+125=180



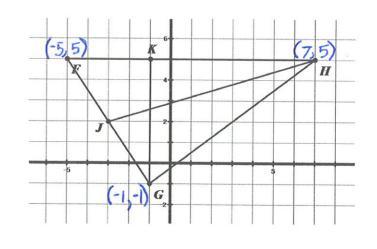
Since same-side interior angles are supplementary, the lines are parallel, which makes TVWX a trapezoid.

If HJ is a median, then J is the midpoint of FG.

$$Midpoint = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$J = \left(\frac{-5+1}{2}, \frac{5+1}{2}\right)$$

$$J = (-3,2)$$



If GK is an altitude, then it is perpendicular to FH.

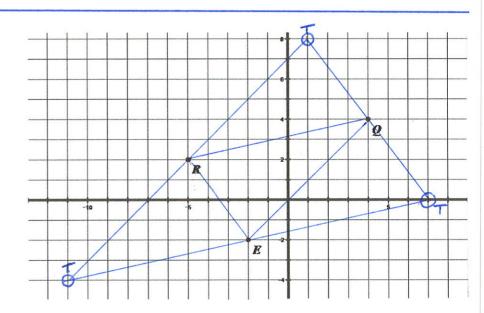
Simply start at G on the graph and travel directly up

until you intersect FH at point K. The coordinates are:

$$K = (-1, 5)$$

#9

There are three possible locations for point T that will ensure the two sets of parallel sides a parallelogram requires. To find them, use the fact that parallel lines have the same slope.



LT opposite LE

To get to Q from E, you travel 6 units up and 6 units right. For a parallel segment, travel 6 units up and 6 right from point R.

$$T = (1,8)$$

LT opposite LR

To get from R to Q, travel up 2 units and 9 units right. Follow that path from E to get another set of coordinates for T.

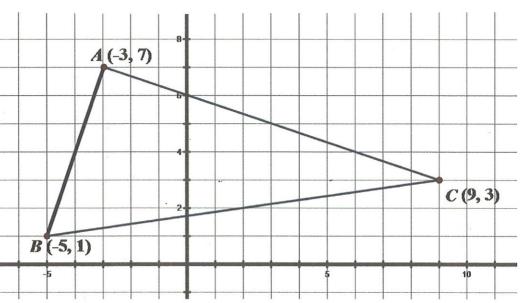
LT opposite LQ

To get to R from Q, you travel 2 units down and 9 units left. Follow that path from E to get the last possible location for T.

$$T = (-11, -4)$$

The circumcenter of a triangle is equidistant from its vertices, so it is the center of the circle that circumscribes it. Therefore, you must find the intersection of the triangle sides' perpendicular bisectors.

Suppose We find the I bisectors of segments AC and BC, and then find their point of intersection.



The midpoint of AC is:

$$\left(\frac{-3+9}{2}, \frac{7+3}{2}\right) \longrightarrow (3,5)$$

The slope of AC is:

The perpendicular bisector must contain the point (3,5) and have slope 3.

$$Y = mx + b$$

 $5 = 3(3) + b$
 $5 = 9 + b$
 $-4 = b$

The midpoint of BC is:

$$\left(\frac{-5+9}{2},\frac{1+3}{2}\right)$$
 $\left(2,2\right)$

The slope of BC is:

$$\frac{3-1}{9-5} = \frac{2}{14} = \frac{1}{7}$$

The perpendicular bisector must contain the point (2,2) and have slope -7.

$$2 = -7(2) + b$$

 $2 = -14 + b$
 $16 = b$

Now, set the two equations equal to each other to find the point of intersection.

$$3x-4 = ^{-}7x+16$$

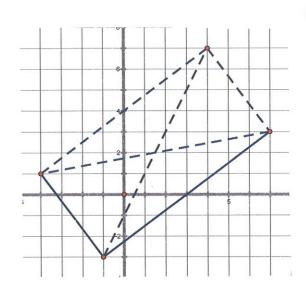
 $3x = ^{-}7x+20$
 $10x = 20$
 $x = 2$

If
$$x=2$$
 then:
 $y=3(2)-4$
 $y=6-4$
 $y=2$

#11

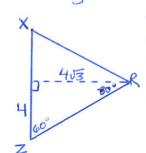
For a more visual solution, use the idea of parallel sides to find the 4th vertex of the rectangle, draw in the diagonals, and find where they cross. Or, using the fact that diagonals of a rectangle bisect each other, simply find the midpoint of the diagonal connecting (-4,1) and (7,3).

$$P = \begin{pmatrix} -\frac{4+7}{2}, \frac{1+3}{2} \end{pmatrix} = \begin{pmatrix} 1.5, 2 \end{pmatrix}$$



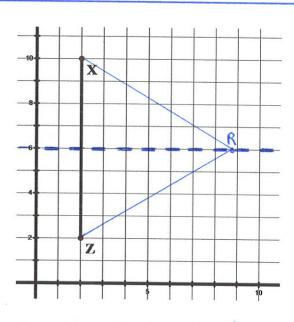
#12

If \triangle XZR is equilateral, R will lie somewhere on the line y=6 (halfway up \overline{XZ}). It will also form two $30^{\circ}-60^{\circ}-90^{\circ}$ triangles:



To find the length of the triangle's altitude, multiply the small leg by J3.

45 = 6.9



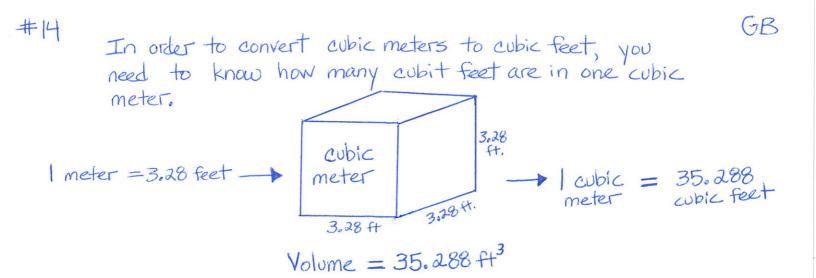
Since the X-coordinate of X and Z is 2, simply add 6.9 to get the X-coordinate of R. $R \rightarrow (8.9, 6)$

#13

Convert each population entry to scientific notation, precise to one digit (see table). Then you can identify the requested years.

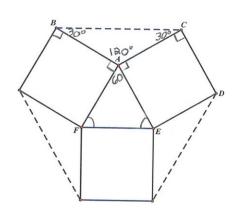
year	Population
1901	238,396,327
1911	252,093,390
1921	251,321,213
1931	278,977,238
1941	318,660,580
1951	361,088,090
1961	439,234,771
1971	548,159,652
1981	683,329,097
1991	846,421,039
2001	1,028,737,436

1 × 109



 $2.5 \text{ m}^3 \times \frac{35.288 \text{ ft}^3}{1 \text{ m}^3} = 88 \text{ ft}^3$

Notice that at each vertex of the equilateral \triangle (point A, for example), four angles surround the point. Two are 90° angles and one is a 60° angle. That leaves 120° for LBAC, which means \triangle BAC is obtuse. Therefore, its longest side is \overline{BC} . Since the hexagon's sides are not all congruent (half are the length of \overline{BC} and half are the length of the square's sides):



NOT EQUILATERAL

The obtuse triangles are isosceles, with base angles measuring 30° Each of the hexagon's vertices are comprised of a 30° angle and a 90° angle. Since they are all 120°, the hexagon is:

EQUIANGULAR

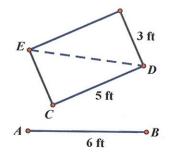
As the box is being tipped, its tallest part will be along the diagonal. Use the Pythagorean Theorem to find out if it is less than 6 feet.

$$3^{2} + 5^{2} = \overline{ED}^{2}$$

$$9 + 25 = \overline{ED}^{2}$$

$$34 = \overline{ED}^{2}$$

$$5.83 = \overline{ED}$$



Since 5.83 is less than 6, the box can be tipped.